

Dimensional analysis

Answers to additional problems

- 36.1** The label should be completely dimensionless and without a factor. We treat the data as an equation. For example, we start with the equation Applied pressure $p = 1 \times 10^5$ Pa. We divide both sides by the unit Pa and multiply both sides by the inverse of $\times 10^5$ which is clearly 10^{-5} . This yields 10^{-5} Applied pressure $p / \text{Pa} = 1$. If this statement is correct for one datum, it will be correct for a column heading.
- 36.2** We start with pressure p because the variable is pressure. Because the unit of pressure in this example is the bar, we write, pressure, p / bar . This way, the label is completely dimensionless.
- 36.3** Inserting known units, $[\text{J mol}^{-1}] = [\text{J mol}^{-1}] - [\text{K}][\Delta S^\ominus]$.
To be dimensionally correct, each of these three terms must be dimensionally identical. Therefore, $[\text{K}][\Delta S^\ominus]$ is dimensionally equivalent to $[\text{J mol}^{-1}]$, $\text{K} \times \Delta S^\ominus = \text{J mol}^{-1}$. Dividing both sides by K yields, $\Delta S^\ominus = \text{J K}^{-1} \text{ mol}^{-1}$.
- 36.4** 1. One atm = $\frac{101\,325}{10^5}$ bar = 1.013 2 bar (to 4 s.f.)
2. One bar = $\frac{10^5}{101\,325}$ atm = 0.986 9 atm (to 4 s.f.)
- 36.5** Current $I = dQ/dt$, where Q is charge in coulombs and t is time. Rearranging yields $dQ = I \times dt$. Inserting units, $[\text{C}] = [\text{A}][\text{s}]$ so a Coulomb has the compound unit, A s.
- 36.6** The chemist should start by defining molar mass, saying,

$$\text{mass} \div \text{amount of material, } m \div n$$

Inserting units, $M = \frac{[\text{kg}]}{[\text{mol}]}$ so molar mass has the units of kg mol^{-1} .

Chemists are permitted to deviate from the SI system of units and almost always cite a molar mass in g mol^{-1} .

- 36.7** The Nernst equation is, $E = E^\ominus + \frac{RT}{nF} \ln \left(\frac{[\text{O}]}{[\text{R}]} \right)$

Inserting units, $[\text{V}] = [\text{V}] + \frac{[\text{J K}^{-1} \text{ mol}^{-1}] \times [\text{K}]}{[1][\text{C mol}^{-1}]} \times [1]$

Cancelling yields, $[\text{V}] = [\text{J C}^{-1}]$. The definition of an Ampère A is a coulomb C per second (see the answer to Additional Problem 36.5). A coulomb has the units of A s and C^{-1} has the units $\text{A}^{-1} \text{ s}^{-1}$ or $(\text{A s})^{-1}$.

The compound unit of the joule is $\text{kg m}^2 \text{ s}^{-2}$ (see Table 36.2). Substituting yields, $[\text{V}] = [\text{kg m}^2 \text{ s}^{-2}] [\text{A}^{-1} \text{ s}^{-1}]$. The SI units of potential are therefore $[\text{kg m}^2 \text{ s}^{-3} \text{ A}^{-1}]$.

- 36.8** Rearranging the equation, $k_b = R \div N_A$. Inserting units, $[k_b] = \frac{[\text{J K}^{-1} \text{ mol}^{-1}]}{[\text{mol}^{-1}]}$. Cancelling yields k_b in $[\text{J K}^{-1}]$.

36.9 The Clapeyron equation is, $\frac{dp}{dT} = \frac{\Delta H}{T \Delta V_m}$. The subscripted m on ΔV means molar volume so m^{-3} . Rearranging to make dp the subject yields, $dp = \frac{dT \Delta H}{T \Delta V_m}$.

Inserting unit terms, $[dp] = \frac{[\text{K}] [\text{J mol}^{-1}]}{[\text{K}] [\text{m}^3 \text{mol}^{-1}]}$. Cancelling yields, $[\text{J m}^{-3}]$. From Table 36.2, the SI units of the joule are, $\text{kg m}^2 \text{s}^{-2}$.

Substituting for J gives $[\text{Pa}] = [\text{kg m}^2 \text{s}^{-2}] [\text{m}^{-3}] = [\text{kg m}^{-1} \text{s}^{-2}]$ which is the same as that in Table 36.2.

36.10 Inserting units, $[C_p] = \frac{[\text{J mol}^{-1}]}{[\text{K}]} = [\text{J K}^{-1} \text{mol}^{-1}]$. The joule (in the SI system) is $[\text{kg m}^2 \text{s}^{-2}]$. Therefore, $[C_p] = [\text{kg m}^2 \text{s}^{-2} \text{K}^{-1} \text{mol}^{-1}]$.